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## APPLICATION OF SIMILARITY METHOD AND DIMENSIONAL ANALYSIS IN DETERMINING THE PERFORMANCE PARAMETERS OF AGITATOR PADDLES FOR CALTEX AQUATEX 3180 CUTTING OIL

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### Abstract:

*Aquatex 3180 is the general purpose soluble oil, formulated for use in a wide variety of machining operations. In fact, the natural diffusion in the liquid is very slow, especially the mixing ratio, and the homogeneity of the solution is difficult to achieve according to the manufacturer's recommendation. Hence, the agitator is required to improve the uniformity of the solution in that the obtained cutting fluid can be effectively used in machining processes to fulfill the role of cooling and lubricating. In this work, the application of the similarity method and dimensional analysis for studying agitator model for mixing Aquatex 3180 cutting oil to build the set of input parameters in the experimental process. The results reveal that the input parameters in the study of the agitator model using 9 similarity criteria  $\pi_i$  ( $i = 1 \dots 9$ ) instead of 12 independent parameters. In addition, the standard  $\pi_2$  can characterize the displacement properties of the fluid flow considering the influence of gravity. It means that the number of experiments reduce but still ensure that many experimental input parameters are still guaranteed, therefore ensuring proper description of the actual operation of the machine.*

**Keywords:** Caltex Aquatex 3180; Similarity Method; Dimensional Analysis; Agitator; Mixing; Cutting Oil.

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### 1. Introduction

Currently, the Caltex Aquatex 3180 cutting oil is widely used to lubricate and cool in mechanical production. It brings out the efficient machining, grinding, and hard cutting: High detergency performance keeps grinding wheels free of grit and fines, and flushes and settles chips. Low foaming tendency is an advantage in high speed operations. Also, high precision and surface finish: High performance heat transfer and reduced tool/workpiece friction ensures precise dimensional accuracy and good surface finish on parts [1, 23-25].

However, this solution is in the concentrated form and is needed to be diluted according to a recommended rate before use. In fact, the natural diffusion in the liquid is very slow, especially the mixing ratio, and the homogeneity of the solution is difficult to achieve according to the manufacturer's recommendation [15]. Accordingly, the agitators are needed to improve this. However, it can lead to waste of input energy, and the reduction of product quality when the system is not suitable. Therefore, it is necessary to have more studies to determine the specification of the Caltex Aquatex 3180 lubricant agitator model to improve the uniformity of the solution [2-8, 13].

A convenient and common method for studying the complicated systems and processes theoretically and experimentally with diverse and not perfectly known parameters is the similarity theory (also called dimensional analysis) [9–12]. The essence of this theory is in combining the independent variables and quantities into dimensionless quantities (i.e. similarity criteria) of certain structure, which are generalized variables and parameters of the problems concerned. The quantitative interrelations between these dimensionless quantities are further revealed [10]. The method of similarity method and dimensional analysis is used to determine the input allowable experimental parameters to replace the independent parameters by the similarity criterion by comparing the components in the line conservation program together. If a component as a unit is chosen and other components are taken to compare with it, there will be an independent set of criterion that characterizes the uniformity of processes occurring in the system. Thus, it is possible to reduce the number of experiments but still survey much input information independently. This method has recently applied in different fields of studies [16-18, 20]. The dimensional analysis was used in electrostatic precipitators (ESP) model building, showing both the reduction in effort and more effective modeling that can result. The obtained results show that it allows to reduce the number of parameters necessary for defining the ESP performance, provides a reliable scaling-up of the desired operating conditions from the pilot-scale to full-scale plant (based on the invariance of the pi-space) as well as a consistent extrapolation within the range covered by dimensionless numbers, and gives a greater flexibility in choice of parameters [19].

However, the literature suggests that there are almost no studies of the application of the similarity method and dimensional analysis for studying agitator model for mixing cutting oil. Therefore, in this paper, the authors are motivated to make the study of the application of the similarity method and dimensional analysis to build the set of input parameters in the experimental process for studying agitator model of the Caltex Aquatex 3180 cutting oil. From the results, they reveal that the input parameters in the study of the agitator model using 9 similarity criterions  $\pi_i$  ( $i = 1 \dots 9$ ) instead of 12 independent parameters. Among them, the standard  $\pi_2$  can characterize the displacement properties of the fluid flow considering the influence of gravity. This allows to reduce the number of experiments but still ensures that many experimental input parameters are still guaranteed, therefore ensuring proper description of the actual operation of the machine.

## 2. Materials and Methods

### 2.1. The Properties of Mixing Process and Technological Parameters

#### 2.1.1. Kinetic Mode of Mixing Process

In order for the agitator to rotate at the desired speed, it is necessary to provide the power to overcome the resistance of the solution. Many theoretical as well as experimental studies show that the power provided for stirring mechanism depends mainly on:

- Type of stirring mechanism;
- Speed of stirring mechanism;
- The rheological properties of the solution
- Geometric features of the container

Using the method of dimension analysis of collected data, there is a relationship between the following quantities [21,22].

$$+ \text{Reynoldscriterion:} \quad R_e = \frac{d^2 N \rho}{\mu} \quad (1)$$

$$+ \text{Froudecriterion:} \quad F_r = \frac{N^2 D}{g} \quad (2)$$

$$+ \text{Froude criterion:} \quad P_o = \frac{P}{N^3 D^5 \rho} \quad (3)$$

Where:

Po: Power factor of the mixing power

P: Stirring power, kw;

N: Motor speed, s<sup>-1</sup>;

D: Diameter of the paddles, mm;

g: Gravitational acceleration, m/s<sup>2</sup>;

μ: Kinetic viscosity, mPa.s (cst)

ρ: Density of liquid, kg/m<sup>3</sup>;

#### 2.1.2. Mixing Time

Mixing time is one of the most important parameters in liquid-liquid mixing because it is also the time required to obtain a desired homogeneity in the mixing tank (Montante et al, 2005; Jakobsen, 2008). The diameters of paddles and mixing tanks, liquid viscosity, and so on are effective parameters for determining mixing time (Jakobsen, 2008; Doran, 1995). Patwardhan and Joshi (1999) also determined the mixing time with about 40 types of axial flow propellers.

The impellers vary in twist angle, width, diameter, position and pump direction. The results showed that the use of inclined turbine blades led to the shortest mixing time. Determining mixing time by Zhao et al. (2011) in an oil and water system shows an increase in mixing time because

oil is lighter than water, so it tends to combine and stay on the surface, resulting in poor dispersion of oil and increasing mixing time.

Pip and his colleagues [14] suggested the following correlations to calculate the mixing time for chaotic mixing:

$$t_m = 5.91d_v^{2/3} \left(\frac{\rho V}{P}\right)^{1/3} \left(\frac{T}{D}\right)^{1/3} \quad (4)$$

Where:

T: diameter of mixing tank, mm

D: diameter of the impellers, mm

V: liquid volume, l

P: mixing power, kw

### 2.1.3. The Density and Viscosity of Liquid

Bouwman et al. [15] studied the effect of density and viscosity on mixing time when they were mixed under different conditions (paddles, machines, and mixing speed) as well as the position of the liquid supplement to the second liquid in the mixing chamber. The obtained results revealed an observation when an added liquid is lighter than the liquid in the mixing chamber, it will significantly increase the mixing time and lower mixing speed. In addition, as the liquid is added near the paddles, the mixing time is not different.

### 2.1.4. The Homogeneity

- The mathematical model of Паскатова E.A as below:

$$V_c = A(\omega t)^B + Clg(\omega t) = f\left(\frac{l_1}{l}, \frac{\gamma_1}{\gamma}, \frac{g}{l\omega^2}, \varphi, \omega t\right) \quad (5)$$

Where:

A, B, C- the function of dimensionless quantities

$l_1, l$  - the size of components

$\gamma_1, \gamma$  - intensity of components

$g$  - gravitational acceleration

$\omega$  - angular velocity

$\varphi$ - container coefficients of the agitators

$t$  - mixing time

## 2.2. The Similarity Model and Dimensional Analysis

For researching in the field of design and manufacturing machines, most researchers conduct multi-factor experiments with independent input parameters [3,7]. The more the number of input parameters and the number of experiments is conducted, the more reliable the experimental results are. However, the process of stirring liquids is a very complex process, and furthermore, conducting many experiments with independent parameters does not only take a lot of time and money in research, but also cannot fully describe physical processes. This problem can be solved

by applying the similarity method and dimension analysis. During conducting the experiments, independent parameters can be replaced by similarity criterions by selecting a component as a unit and comparing other components with it. Then, the set of independent criterions will characterize the similarity of the process occurring in the system. This method helps to reduce the number of experiments but still possesses the ability to survey much information independently to ensure the reliability of the experimental results.

The application of the similarity method and dimension analysis to study the agitator of Caltex Aquatex 3180 cutting fluid is a new application. From that, the author builds the set of criterions as a basis for conducting experiments on the agitator of Caltex Aquatex 3180 cutting fluid.

### 2.3. The Application of the Similarity Method and Dimension Analysis to Determine the Experimental Input Parameters on The Agitator of Caltex Aquatex 3180 Cutting Fluid

#### Determination of Similarity Criterions

After studying the working characteristics of the agitator, the mixing productivity Q depending on the following main factors is determined:

$$Q = f(D, \omega, L_c, T, \varepsilon, h, d, \alpha, \rho, \mu, g) \tag{6}$$

The quantities in the above equation are shown in the table below

Table 1: Basic parameters related to the mixing process

<u>No.</u>	<u>Quantity</u>		<u>Dimension</u> $M^\mu.L^\lambda.T^\tau$		
	<u>Symbol</u>	<u>Name</u>	$\mu$	$\lambda$	$\tau$
1	D	The diameter of the paddle	0	1	0
2	$\omega$	Angular velocity of mixing shaft	0	0	-1
3	$L_c$	Length of mixing shaft	0	1	0
4	T	Diameter of mixing tank	0	1	0
5	$\varphi$	Container coefficient	0	0	0
6	H	Distance between the paddle and tank bottom	0	1	0
7	D	Diameter of mixing shaft	0	1	0
8	A	Helical angle between the paddle and mixing shaft	0	0	0
9	Q	Productivity	1	0	-1
10	$\rho$	Density	1	-3	0
11	$\mu$	Kinematic viscosity	1	0	-3
12	G	Gravitational acceleration	0	1	-2

In the above table:

M - mass, kg

L - length, m

T - time, s

Choose the basic quantities: D,  $\rho$ , g; Their determinant is

$$\Delta = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -3 & 0 \\ 0 & 1 & -2 \end{bmatrix} \neq 0$$

This proves that the basic quantities chosen are appropriate.

According to the dimension equation, the obtained criteria will be:

$$\pi_1 = \frac{Q}{\rho\sqrt{gD^5}}; \pi_2 = \omega\sqrt{\frac{D}{g}} = F_r; \quad \pi_3 = \frac{L_c}{D}; \quad \pi_4 = \frac{h}{D};$$

$$\pi_5 = \frac{T}{D}; \pi_6 = \frac{d}{D}; \pi_7 = \alpha; \pi_8 = \mu; \quad \pi_9 = \varepsilon;$$

Where:  $\pi_2$  is Frut ( $F_r$ ) criterion when the displacement properties of flows are studied by considering the influence of gravity. The  $F_r$  criterion is the ratio between the inertial force and the gravitational force.

$$\Pi_2 = \frac{p}{v^2 \cdot \rho} = E_u; \quad \Pi_3 = \frac{\mu}{v \cdot D \cdot \rho} = \frac{1}{R_e};$$

According to Buckingham Pi Theorem, the equation for  $\pi_1$  is written as:

$$\pi_1 = \frac{Q}{\rho\sqrt{gD^5}} = \varphi\left(\frac{\omega^2 D}{g}, \frac{L_c}{D}, \frac{T}{D}, \frac{h}{D}, \frac{d}{D}, \alpha, \mu, \varepsilon\right) \quad (7)$$

To reduce the input parameters, the independent parameters in Table 1 are replaced with the criteria as equation (7). When conducting the experiments with the similarity criteria on the agitator model with the same condition ( $D, d, T, L_c, \mu, \varepsilon$  constant). The changing parameters are  $\omega, h, \alpha$ , which characterize the criteria respectively:

$$\pi_2 = \omega\sqrt{\frac{D}{g}} = F_r; \quad \pi_4 = \frac{h}{D}; \quad \pi_7 = \alpha.$$

This is also the input parameters when conducting the experiments

### 3. Results and Discussions

The criteria affecting the mixing process of the solution are given by the equation (7).

The above analysis shows that the input parameters in studying the model of agitator include 9 similarity criteria  $\pi_i$  ( $i = 1 \div 9$ ) instead of 12 independent parameters (seen in Table 1). It can help

to reduce the number of experiments while still providing many input parameters as a basis for determining and evaluating their influence on the uniformity of the solution;

Three obtained criteria  $\pi_2$ ,  $\pi_4$ ,  $\pi_7$  are the numbers included in the study of mixer model. In particular, the  $\pi_2$  is the Froude criteria, which characterizes the dynamics that is put into the experiment, which allows for increasing the accuracy of the experimental model. For the obtained results, the experiments were carried out and their results will be discussed in detail in the next paper.

#### 4. Conclusions and Recommendations

The similarity method and dimension analysis were successfully applied for the study of the application of the similarity method and dimensional analysis to build the set of input parameters in the experimental process for studying agitator model of the Caltex Aquatex3180 cutting oil. Based on the results of the present experimental investigation, the following conclusions can be drawn:

- 1) The similarity method and dimension analysis are the scientific research method that helps to define and explain the general rules of phenomena and processes that occur and establish the relationship for studying the system.
- 2) On the basis of analyzing the influencing factors for solution mixers, the similarity criteria and the criterion equations are calculated and built to fully describe the physical process during mixing (equation 7). At the same time, they propose three basic criteria as input parameters in experiment  $\pi_2$ ,  $\pi_4$ ,  $\pi_7$ ). This is the basis for building experimental models in accordance with research objectives.
- 3) The input parameters in the study of the model of liquid mixers use 9 similarity criteria  $\pi_i$  ( $i = 1 \dots 9$ ) instead of using 12 independent parameters (as shown in Table 1). Among them, the criterion  $\pi_2$  can characterize the displacement properties of the fluid flow considering the influence of gravity. This helps to reduce the number of experiments but still ensure that many input experimental parameters can investigate while ensuring proper description of the actual operation of the machine.

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